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Improving the Multi-Restart Local Search Algorithm by Permutation Matrices and Sorted Completion Times for the Flow Shop Scheduling Problem

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Abstract—Iterated local search (ILS) is a metaheuristic used successfully to solve the flow shop scheduling problem. In particular, the multi-restart ILS (MRSILS) is an easily implementable algorithm which obtains good results. In this paper, we modify the MRSILS algorithm in two ways. First, small changes in the initial solution are generated by permutation matrices in order to improve it before using the MRSILS. Second, a minor variation is made in the strategy of the MRSILS. Sorted completion times are taken to select the job to be inserted in new positions to obtain a better scheduling. The original MRSILS and both modifications are evaluated with well-known benchmark instances. The experiments show that the new modifications produce slightly better results than the original one, especially for a large number of jobs.

Keywords: Flow shop scheduling problem, iterated local search, permutations, work time costs

1. Introduction

The flow shop scheduling is a classic combinatorial problem established by Johnson in [1]. In this problem, n jobs must be processed on m machines, where each machine is required to process the set of all jobs in the same order. The most common objective in this problem is to minimize the completion time of the last job, or makespan.

Many evolutionary methods have been proposed for makespan minimization. Some of them are based on the modification of continuous evolutionary algorithms. For instance, recent modifications of particle swarm optimization methods have been proposed in [2], [3], [4], and a bee colony algorithm has been presented in [5].

These are only a few examples of the great number of papers devoted to adapt evolutionary and metaheuristic algorithms to minimize the makespan in the flow shop scheduling problem. Very often these papers present complex algorithms in order to construct factible and better solutions. The basic operations in these algorithms, however, are a mixture and/or extensions of job insertions and swaps.

Past research shows that simpler algorithms are able to obtain effective results without need of complex strategies.

In particular, the iterated local search method (ILS) has been applied in the minimization of the total flow time for the flow shop scheduling problem [6]. This method has been recently improved using multi-restart points (MRSILS), showing better results than many more intricate and sophisticated metaheuristics [7]. This method is only based in insertions of jobs; without considering swaps.

This paper takes the MRSILS algorithm proposed by Dong et al. in [7] in order to minimize the makespan of the flow shop scheduling problem. Then, two modifications are presented. The first one consists of applying a matrix which defines job permutations to improve a given initial solution. This improved solution is passed to the MRSILS algorithm to obtain a final result. This modified algorithm is called MRSILS_PM.

The second modification is a slightly change in the strategy of the MRSILS, where the job to be inserted is selected sorting the differences of completion job times. For this reason, this modification is called MRSILS_SD.

The three algorithms have been evaluated taking the benchmark instances proposed in [8] and [9], which can be downloaded as the data file *flowshop1* from the web site OR Library.¹ The results show that MRSILS_PM and MRSILS_SD have obtained slightly better results than the original MRSILS in minimizing the execution time and/or the makespan.

2. Flow shop scheduling problem

The flow shop scheduling problem consists of the assignment of a set of n jobs $W = \{J_1, \ldots, J_n\}$, each job J_i is composed of a set of operations $J_i = \{O_{i1}, \ldots, O_{im}\}$ processed by a set of machines $M = \{M_1 \ldots M_m\}$. Every operation O_{ij} has associated a value T_{ij} that represents the processing time of operation O_{ij} ; for $1 \le i \le n$ and $1 \le j \le m$. Each machine can process only one job at a time. It is assumed that the machine sequence is identical for all jobs, and the job sequence is the same for all machines.

¹http://people.brunel.ac.uk/~mastjjb/jeb/orlib/flowshop info.html. Consulted in January 27th, 2014.

Therefore, a job schedule is represented as a permutation $\pi = \{\pi_1, \ldots, \pi_n\}$ of W. The completion time of the operation O_{ij} is indicated by C_{ij} . The objective of the flow shop scheduling problem is the minimization of the makespan C_{max} , or the completion of the last operation in π .

The model of the flow shop scheduling problem can be defined in the following way:

$$C_{\pi_{1}1} = T_{\pi_{1}1}$$

$$C_{\pi_{1}j} = C_{\pi_{1}j-1} + T_{\pi_{1}j}$$

$$C_{\pi_{i}1} = C_{\pi_{i-1}1} + T_{\pi_{i}1}$$

$$C_{\pi_{i}j} = \max\{C_{\pi_{i-1}j}, C_{\pi_{i}j-1}\} + T_{\pi_{i}j}$$
(1)

where $i \in \{2, \ldots, n\}$ and $j \in \{2, \ldots, m\}$. Thus $C_{max} = C_{nm}$.

3. MRSILS algorithm

The framework of the MRSILS algorithm is very simple [7]. First, a well-known heuristic is applied in order to generate a *good* initial solution. This paper applies the NEH method described in [10], which constructs a solution π in negligible time.

The MRSILS algorithm improves the solution by inserting a selected job into different positions of π to generate a new solution π' . If a better solution is obtained, then π is replaced by π' .

Let π^* be the best solution found by the algorithm. In order to avoid that π^* be trapped in a local optimum, the search space is extended by generating restart solutions from a set Π (or pool) of solutions. This pool keeps the best qsolutions calculated so far. If the MRSILS algorithm does not improve the solution after n iterations, the local optimum π is added to Π if it is not already there. If Π has more than q solutions, the worst solution of the pool is deleted.

When Π is not full, the restart solution is generated from π^* ; otherwise, a solution π' is randomly chosen from Π . The selected solution is perturbed by inserting one randomly chosen job into another randomly chosen position. In this way, a new restart solution π is defined.

Figure 1 shows the pseudocode of the MRSILS algorithm taking the parameters specified in [7].

4. Permutation matrix

The MRSILS algorithm is only based on insertions. It can be considered as an algorithm which performs small changes in every solution in order to achieve an improvement. So the MRSILS algorithm is suitable to refine solutions.

The application of swaps and permutations of jobs, however, are useful to improve an initial solution at the beginning of the optimization process. These operations may produce the exploration of a bigger space search in order to obtain a better schedule which can be refined after with the MRSILS.

These swaps and permutations can be specified in a matrix M, where it has as many rows as n (number of jobs) and r

1: Set q = 20, lim = 10002: Set cnt = 0, flag = 0, $\Pi = \emptyset$ 3: Generate π^* using NEH and set $\pi = \pi^*$ 4: for i = 1 to lim do for j = 1 to n do 5: Find k such that $\pi_k = \pi_j^*$ 6: Insert π_k into other n-1 positions in π , 7: let π' be the best solution from the n-1 generated permutations 8: if π' is better than π then Set $\pi = \pi', cnt = 0$ 9: else Set cnt = cnt + 110: if π is better than π^* then Set $\pi^* = \pi$, flag = 1if cnt = n then 11: 12: if flag = 1 then Set $\Pi = \emptyset$, flag = 013: if $\pi \notin \Pi$ then Add π into Π if $|\Pi| > q$ then 14: Delete the worst π' from Π 15:if $|\Pi| < a$ then Perturb π^* to obtain a new π else 16: Select π' at random from Π and perturb it to obtain a new π if π is better than π^* then 17: Set $\pi^* = \pi$ 18: Set cnt = 019: return π'

Fig. 1: Pseudocode of MRSILS.

columns. Here, r is the number of different solutions to be obtained for the swaps and permutations defined by M.

For a job schedule $\pi = {\pi_1 \dots \pi_n}$, every column j in M defines a new permutation π' . The entry m_{ij} indicates the new place of the job π_i . If $m_{ij} = i$, then $\pi'_i = \pi_i$; that is, the job i in π conserves the same position in π' . Otherwise, for $m_{ij} = z \neq i, \pi'_i = \pi_z$. The job at position z in π changes into position i in π' . Therefore, every column j in M is a permutation of $Z_n = \{1, \dots, n\}$. Since M consists only of permutations of Z_n , it is easily defined and can be applied quickly to π to produce a new schedule.

In order to define the matrix M, we are taking into account four parameters:

- $r \rightarrow$ number of columns
- $\alpha \rightarrow$ proportion of columns which define large changes
- $\gamma \rightarrow$ proportion of permuted jobs for columns (2) defining large changes
- $\delta \rightarrow$ proportion of permuted jobs for columns defining small changes

In Eq. 2, r can be defined as a multiple of q, the size of the pool Π in the MRSILS algorithm. In our experiments,

the best performance has been obtained with r = 10 * q, $\alpha = 0.55$, $\gamma = 0.6$ and $\delta = 0.1$.

```
1: Set r = q * 10, \alpha = 0.55, \gamma = 0.6 \ \delta = 0.1
 2: Set lim = 1000
 3: Generate \pi^* using NEH
 4: for i = 1 to lim do
 5:
        Set \pi = \pi^* and P = \emptyset
        for j = 1 to r do
 6:
            Set a column vector c = Z_n^T
 7:
            Generate a random number s \in [0, 1]
 8:
            if s < \alpha then
 9:
                Permute round(\gamma * n) elements in c
            else
10:
                Permute round(\delta * n) elements in c
            Add the column c to M
11:
12:
        for j = 1 to r do
13:
            Obtain \pi' by permuting \pi according to
            \operatorname{column} j in M
            Add \pi' into P
14:
        Select the best solution \pi' from P.
15:
        if \pi' is better than \pi^* then
16:
            Set \pi^* = \pi'
17:
18: return \pi^*
```

Fig. 2: Pseudocode of PM.

- 1: Set q = 20, $lim_a = 500$, $lim_b = 500$
- 2: Set r = q * 10, $\alpha = 0.55$, $\gamma = 0.6 \ \delta = 0.1$
- 3: Set cnt = 0, flag = 0, $\Pi = \emptyset$
- 4: Generate π^* using algorithm PM with lim_a iterations.
- 5: Improve π^* using algorithm MRSILS with lim_b iterations.
- 6: return π^*

Fig. 3: Pseudocode of MRSILS_PM.

The algorithm that defines and applies the permutation matrix (PM) is presented in Fig. 2. This algorithm takes first an improved solution from the NEH heuristic, where Z_n^T is the transpose of Z_n and round(a) is the closest integer of a real number a. Figure 3 describes the integration of the MRSILS and PM algorithms (MRSILS_PM). This algorithm takes first an improved solution from PM using small and large random permutations. Finally, the best solution is taken from PM and it is refined (or exploited) by the MRSILS algorithm. Notice that half of the iterations are done by PM and the final half are realized by MRSILS.

5. Strategy using sorted completion times

The second modification proposed in this paper is a slight change in the selection of the job to be inserted in the line 6 of the MRSILS algorithm (Fig. 1). In the original algorithm, the job is selected finding the position k in π containing the job j in the current best solution π^* . In the proposed modification, first the completion times of every job in π^* are taken. These completion times define a vector D as follows:

$$D = \{C_{im} : i = 1, \dots, n\}$$
(3)

Equation 3 can be obtained when the makespan is calculated with Eq. 1, therefore, this calculus does not imply an extra numerical work. Then, the differences E between completion times is calculated as follows:

$$E = \{D_{j+1} - D_j : j = 1, \dots, n-1\}$$
(4)

Notice that |E| = n-1 and all the values of E are positive because $D_j < D_{j+1}$ for every j in Eq. 4.

Once calculated Eq. 4, E is sorted in a descending way, where I is the index vector associated with E. That is, the first element of I is the index of the highest element in E; the second element of I is the index of the second highest element in E, and so on.

Take the first index μ in *I*. This index represents the pair of jobs π_{μ} and $\pi_{\mu+1}$ with the greatest completion time difference. A big difference would indicate that these jobs are not well-ordered in π^* , and a best solution could be obtained if one of the jobs is inserted in a different position.

Consequently, each π_{μ} and $\pi_{\mu+1}$ are inserted in the other positions, similar to the process done in the MRSILS algorithm. If some insertion improves the current solution, D and E are also updated. This process is iteratively repeated taking the *i*-th element of I in every step. This modification is called MRSILS_SD. In short, MRSILS_SD takes as criterion the descending sort of completion time differences to select the jobs to be inserted, in order to improve the current schedule. Figure 4 presents the pseudocode of the MRSILS_SD algorithm.

6. Experimental results

The original MRSILS algorithm and the two modifications (MRSILS_PM and MRSILS_SD) have been evaluated taking 29 flow shop scheduling instances commonly used in the literature (car1,..., car8; and rec01, rec03,..., rec43) [8] [9].

The parameters selected to compare the three algorithms are presented in Table 1. For each case, 50 independent runs have been calculated for every flow shop scheduling instance. Table 2 presents the data of each problem: name (N), size (n, m) indicating n jobs and m machines, and their optimum value (O). In order to compare the results, Table 2

1: Set $q = 20$, $lim = 1000$	
2: Set $cnt = 0$, $flag = 0$, $\Pi = \emptyset$	
3: Set $D = \emptyset$, $E = \emptyset$, $I = \emptyset$	
4: Generate π^* using NEH and set π	$=\pi^*$
5: for $i = 1$ to lim do	
6: for $j = 1$ to $n - 1$ do	
7: Set $D = \{C_{im} : i = 1, \dots, n\}$	}
8: Set $E = \{D_{j+1} - D_j : j = 1\}$	$1,\ldots,n-1\}$
9: Set I as the index vector as	ssociated with E
sorted in a descending way	
10: Take index $\mu = I_j$ and inset	rt π_{μ} and
$\pi_{\mu+1}$ into the other position	ns in π ,
let π' be the best solution f	rom the
2n-2 generated permutation	ions
11: Follow algorithm MRSILS	from line 8.
12: return π^*	

Fig. 4: Pseudocode of MRSILS_SD.

Table 1: Parameters to compare the three algorithms.

1	\mathcal{O}
Parameter	Value
Pool size (q)	20
Number of iterations (<i>lim</i>)	1000
Number of iterations for the	500
PM part (lim_a) in MRSILS_PM	
Number of iterations for the	500
MRSILS part (lim_b) in MRSILS_PM	
Number of permutations (r) in PM	200
Proportion of columns (α) in PM	0.55
defining large changes	
Proportion of permuted jobs (γ) in PM	0.6
for columns defining large changes	
Proportion of permuted jobs (δ) in PM	0.1
for columns defining small changes	

also shows the results obtained by each algorithm: minimum (M), mean value (MV) and mean execution time (MET, in seconds). The best results obtained by any of the algorithms are presented in bold. Notice that more than one algorithm may reach the best value in every instance.

Table 4 shows a summary of the results obtained by the algorithms. This table presents the number of times in which each algorithm has obtained the best results.

From Tables 2 and 4, we can see that the three algorithms optimize easily the problems car1 to car8. In these ones, the original MRSILS has the minimum MET. For the problems rec01 to rec41, the three algorithms had similar results to find the optima, and MRSILS and MRSILS_SD have obtained almost the same results in finding the best MV. We can see, however, that MRSILS_SD had a better performance than the other algorithms to find the best M. In particular, MRSILS_SD has outperformed the other algorithms to find a minimum makespan for the greater instances of the rec problems (from rec19 to rec 41). Nevertheless, MRSILS_SD

is a more time-consuming algorithm than the other ones. This is notorious as well in Table 2 for the greater instances of the rec problems. The MET parameter of MRSILS_SD is almost 75% greater than the same parameter of MRSILS in the last three problems.

Finally, it is clear that MRSILS_PM is the fastest algorithm for the rec problems. Actually, MRSILS_PM is executed in almost 50% less time that the original MRSILS for the last three problems in Table 2.

For each of the 12 hardest problems (rec19 to rec41), another set of 50 independent runs have been executed for every algorithm, but taking now lim = 4000. This implies that $lim_a = lim_b = 2000$ in the MRSILS_PM algorithm. Table 3 displays the results of this experiment and Table 5 presents the result summary. In the second experiment, we can see again that MRSILS_PM is faster than the other two algorithms. All the algorithms improved their results, especially the algorithm MRSILS_PM which improves the performance of MRSILS in the *Optimum* and *Best M* parameters. We can notice that MRSILS_SD outperforms the other algorithms in the second experiment as well, mainly in the last three problems.

7. Concluding remarks

The MRSILS is a very simple algorithm capable to obtain very good results in the optimization of the flow shop scheduling problem. On the contrary to more complex methods of optimization, the MRSILS algorithm is only based in insertions, starting from a single initial solution. In this manuscript, two modifications of the MRSILS have been proposed in order to improve its performance.

The first one (MRSILS_PM) consists of executing random permutations in the initial solution. One part of these permutations take into account a minimal part of the jobs, and the other part permutes a greater number of jobs. The experimental results show that this process is faster in a rough 50% than the original MRSILS algorithm for the bigger problems presented in this paper. Besides, MRSILS_PM obtains similar results to MRSILS for the *Best M* parameter.

The second modification (MRSILS_SD) is a small change in the strategy of the original algorithm. It selects the jobs to be inserted according to the difference of completion times between contiguous works. We suppose that bigger differences may indicate bad placed jobs that need to be reallocated in order to improve the solution. The experimental results show that MRSILS_SD outperforms slightly the other algorithms. This performance is not for free, the sorting operation involved in the step 9 of the algorithm (Fig. 4) increases the execution time in a rough 75% compared to the original MRSILS, for the bigger cases.

Future work could consider the implementation of an algorithm where the first part applies the matrix permutation and the second one implements the strategy of differences between completion times.

Table 2. Results of the time algorithms for $t = 1000$.											
N	S	0		MRSILS MRSILS_PM				MRSILS_S			
	(n,m)		M	MV	MET	M	MV	MET	M	MV	MET
car1	(11, 5)	7038	7038	7038	2.29	7038	7038	3.52	7038	7038	3.1
car2	(13, 4)	7166	7166	7166	3.07	7166	7166	3.89	7166	7166	4.29
car3	(12, 5)	7312	7312	7312	2.65	7312	7315.24	3.71	7312	7312	3.71
car4	(14, 4)	8003	8003	8003	3.52	8003	8003	4.14	8003	8003	4.97
car5	(10, 6)	7720	7720	7720	1.91	7720	7720	3.32	7720	7720	2.55
car6	(8,9)	8505	8505	8505	1.31	8505	8505	3.06	8505	8505	1.66
car7	(7,7)	6590	6590	6590	1.01	6590	6590	2.81	6590	6590	1.23
car8	(8, 8)	8366	8366	8366	1.29	8366	8366	3.01	8366	8366	1.64
rec01	(20, 5)	1247	1247	1248.32	7.5	1247	1248.64	6.4	1247	1248.68	11.3
rec03	(20, 5)	1109	1109	1109	7.52	1109	1109	6.4	1109	1109	11.3
rec05	(20, 5)	1242	1245	1245	7.50	1242	1244.88	6.45	1242	1244.94	11.43
rec07	(20, 10)	1566	1566	1566.04	8.91	1566	1567.44	7.4	1566	1566.36	13.65
rec09	(20, 10)	1537	1537	1537	8.79	1537	1537	7.33	1537	1537	13.66
rec11	(20, 10)	1431	1431	1431	8.89	1431	1431	7.39	1431	1431	13.58
rec13	(20, 15)	1930	1930	1933.48	10.28	1930	1934.7	8.43	1930	1932.82	16.04
rec15	(20, 15)	1950	1950	1950.24	10.24	1950	1952.64	8.36	1950	1950.36	15.98
rec17	(20, 15)	1902	1902	1902	10.07	1902	1903.18	8.35	1902	1902.28	16.07
rec19	(30, 10)	2093	2099	2104.44	22.65	2099	2102.92	14.75	2099	2102.84	37.03
rec21	(30, 10)	2017	2020	2044.04	27.81	2021	2045.08	17.29	2020	2040.78	38.35
rec23	(30, 10)	2011	2014	2019.74	28.1	2014	2020.18	17.43	2013	2019.24	39.03
rec25	(30, 15)	2513	2513	2523.3	32.49	2513	2532.24	20.06	2513	2529.26	47.44
rec27	(30, 15)	2373	2378	2389.34	32.62	2378	2392.34	20.14	2377	2389.08	47.84
rec29	(30, 15)	2287	2287	2299.96	32.81	2290	2304.56	20.21	2287	2301.02	47.35
rec31	(50, 10)	3045	3053	3056.94	95.38	3053	3061	51.73	3053	3056.86	143.27
rec33	(50, 10)	3114	3114	3119.06	93.16	3114	3122.04	50.46	3114	3126.46	138.31
rec35	(50, 10)	3277	3277	3277	94.47	3277	3277	51.16	3277	3277	140.64
rec37	(75, 20)	4951	5007	5039.18	395.04	5022	5051.24	205.15	5000	5042.78	681.12
rec39	(75, 20)	5087	5120	5134.84	402.62	5124	5142.86	208.38	5114	5135.9	702.96
rec41	(75, 20)	4960	5018	5049.84	400.62	5026	5058.7	206.99	5017	5048.12	696.53
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Table 2: Results of the three algorithms for l = 1000.

Table 3: Results of the three algorithms for l = 4000.

N	S	0	MRSILS				MRSILS_PI	M		MRSILS_S	D
	(n,m)		М	MV	MET	M	MV	MET	М	MV	MET
rec19	(30, 10)	2093	2096	2100.76	110	2093	2100.08	68.15	2099	2100.2	153.02
rec21	(30, 10)	2017	2020	2038.8	111	2020	2038.62	68.44	2020	2036.18	153.3
rec23	(30, 10)	2011	2013	2017.08	111.2	2011	2017.86	68.85	2013	2018.12	154.95
rec25	(30, 15)	2513	2513	2518.46	127.61	2513	2520.48	78.93	2513	2520.72	187.62
rec27	(30, 15)	2373	2376	2382.04	128.96	2376	2384.68	79.56	2373	2381.7	189.75
rec29	(30, 15)	2287	2287	2292.42	129.14	2287	2293.88	79.72	2287	2292.88	190.1
rec31	(50, 10)	3045	3053	3053.5	377.22	3048	3054.22	204.99	3048	3053.22	560.71
rec33	(50, 10)	3114	3114	3114.68	371.17	3114	3115.96	201.07	3114	3114.16	545.77
rec35	(50, 10)	3277	3277	3277	376.84	3277	3277	204.05	3277	3277	558.32
rec37	(75, 20)	4951	4979	5014.06	1558.13	4993	5022.88	809.45	4964	5016.14	2642.87
rec39	(75, 20)	5087	5120	5128.74	1595.96	5120	5130.14	827.02	5114	5126.92	2712.61
rec41	(75, 20)	4960	4993	5026.7	1575.54	5000	5033.02	822.53	4991	5023.64	2651.83

Table 4: Best results obtained by the algorithms for l = 1000.

Algorithm	Optimum	Best	Best	Best
-	-	Μ	MV	MET
MRSILS	20	23	21	8
MRSILS_PM	20	22	12	21
MRSILS_SD	21	29	19	0

Other possibility is to investigate other criteria in order to select the jobs to be inserted in the different places to improve the current schedule. For instances, the idle times between contiguous jobs or machines.

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Table 5: Best results obtained by the algorithms for l = 400.

			-	-
Algorithm	Optimum	Best	Best	Best
-		M	MV	MET
MRSILS	4	5	5	0
MRSILS_PM	6	8	2	12
MRSILS_SD	5	10	7	0

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